



# Seminario Rubio de Francia

## Conferencia

por

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Título:

*Weakly singular Volterra integral equations of the second kind:  
properties of exact solutions, and approximate solution using  
collocation*

*Resumen:* We describe the structure of exact solutions of weakly singular Volterra integral equations (VIEs) of the second kind, whose integral kernels have factors of the form  $(t - s)^{-\alpha}$  for some constant  $\alpha \in (0, 1)$ . Piecewise polynomial collocation (PPC) approximate solution of this class of problems has been extensively studied in the literature and sharp error estimates are well known. But if one sets formally  $\alpha = 0$ , these error estimates do not coincide with error estimates for PPC for VIEs with smooth kernels, and we correct this anomaly by a new analysis that improves the error bounds for  $\alpha \in (0, 1)$ . Furthermore, we develop a general theory of PPC for variable-exponent weakly singular VIEs (i.e.,  $\alpha = \alpha(t) \in [0, 1)$ ), including existence, uniqueness, and regularity theory for the exact solutions of these problems.

Fecha: Jueves, 5 de diciembre de 2024

Hora: 12:10 horas

Lugar: seminario Rubio de Francia, edificio de Matemáticas, primera planta

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